



# Operationalizing Declarative and Procedural Knowledge

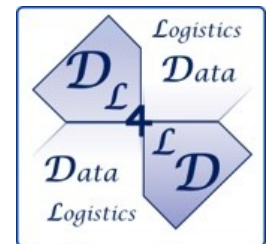
a benchmark on Logic Programming Petri Nets (LPPNs)

CAUSAL2020 Workshop on Causal Reasoning and Explanation in Logic Programming @ ICLP2020

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# Problem: reasoning with cases

- Regulations concern **systems of norms**, that in abstract, in a fixed point in time, may be approached atemporally.
- However, when applied, regulations deal with a **continuous flow of events**.
- Prototypical encounter: legal cases.
- More general but similar problem: narratives, stories.

# Problem: reasoning with cases

While John was walking his dog, the dog ate Paul's flowers.



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The owner of an animal has to pay for the damages it produces.  
(example of underlying norm)

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A conceptual gap exists between the concrete domain and the legal abstraction that applies on it.

While John was walking his **dog**, the dog **ate** Paul's **flowers**.

**dogs are animals**

**flowers are objects**

The owner of an **animal** has to pay for the **damages** it produces.

**destruction is damage**

**eating an object destroys the object**

While John was walking his **dog**, the dog **ate** Paul's **flowers**.

some connections are **terminological** (e.g. taxonomical relations)

other provides **causal** meaning

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**flowers are objects**

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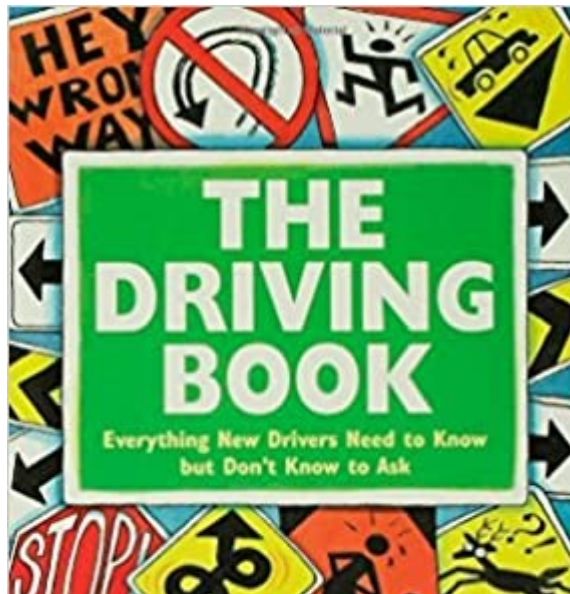
**destruction is damage**

**eating an object destroys the object**



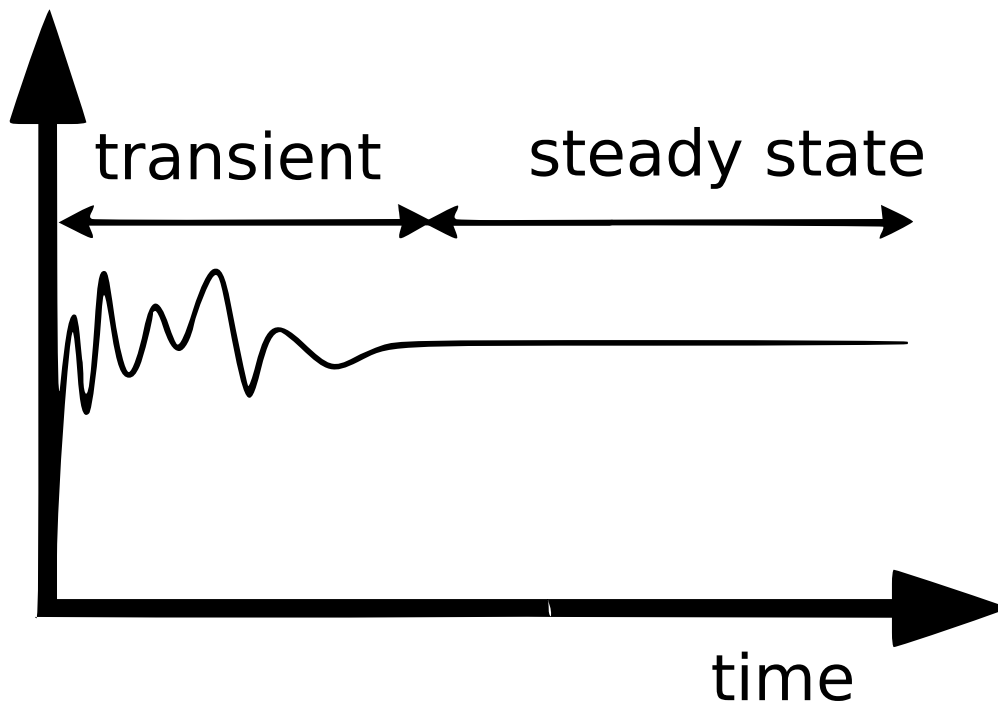
# Types of Knowledge

- **Declarative knowledge**, concerning objects (physical, mental, institutional) and their logical relationships—typically reified by means of symbols
- **Procedural knowledge**, concerning patterns of events/actions, mechanisms, or processes (involving objects)—often tacit, internalized



# Perspectives on Modelling

- Physical systems can be approached from **steady state** (equilibrium) or **transient** (non-equilibrium, dynamic) perspectives



- Steady states descriptions **omit** transient characteristics

ex. Ohm's Law.  $V = R * I$

# Specifying transients and steady states

- Possible analogies:
  - *steady state* approach with
    - Logic
    - **Declarative** programming

focus on  
**What**

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**What**

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Petri Nets!

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Answer Set  
Programming



focus on  
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- *transient* approach

- Process modeling
    - **Procedural** programming



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Petri Nets!

# Specifying transients and steady states

- Possible analogies:

- *steady state* approach

- Logic
- **Declarative** programming

- *transient* approach

- Process modeling
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Answer Set  
Programming

focus on  
**What**

+

focus on  
**How**

*logic programming petri nets*

= **LPPNs**

Petri Nets!

# Logic Programming Petri Nets

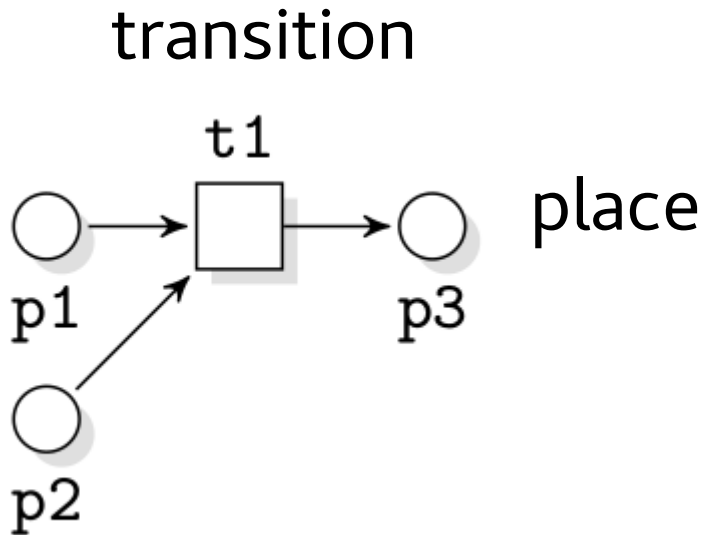


# Logic Programming Petri Net (LPPN)

- An LPPN consists of three components:
  - a procedural net (places, transitions) ← **causal mechanisms**
  - a declarative net for places ← **logical dependencies between objects**
  - a declarative net for transitions ← **logical dependencies between events**

# Procedural LPPN

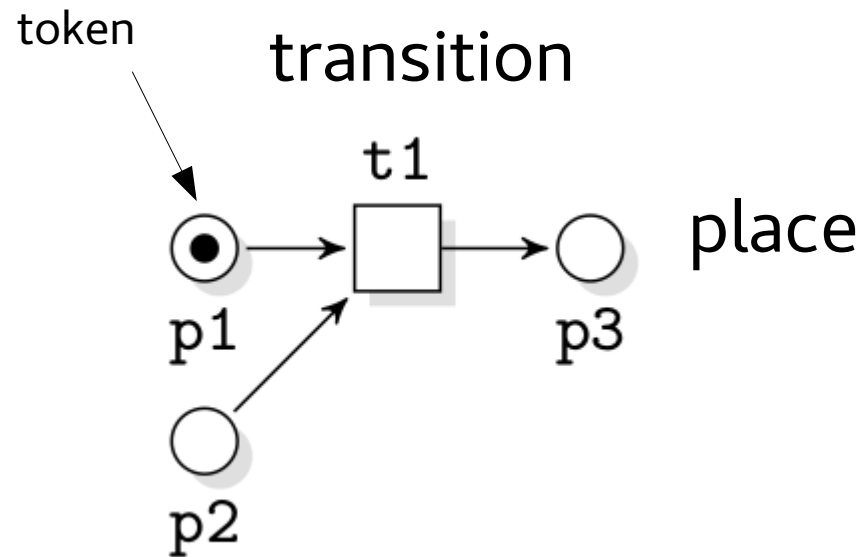
(same as Condition/Event PN)



- Petri net: bipartite directed graph made of **places** (circles) and **transitions** (boxes).

# Procedural LPPN

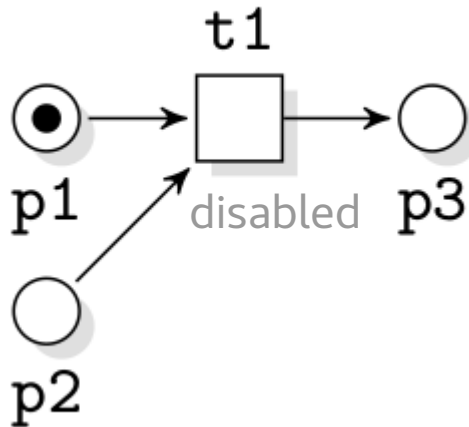
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- **tokens** may occupy places.

# Procedural LPPN

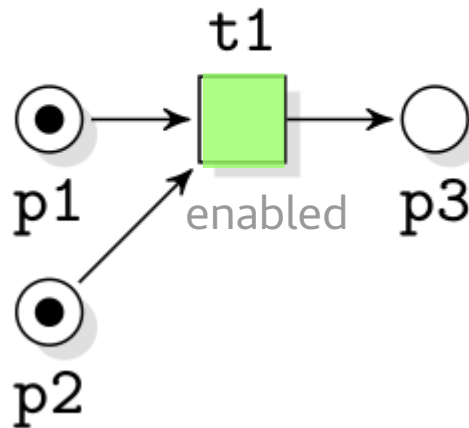
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- Execution semantics (*token game*): if any of its input places is not occupied, the transition is **disabled**. It cannot **fire**.

# Procedural LPPN

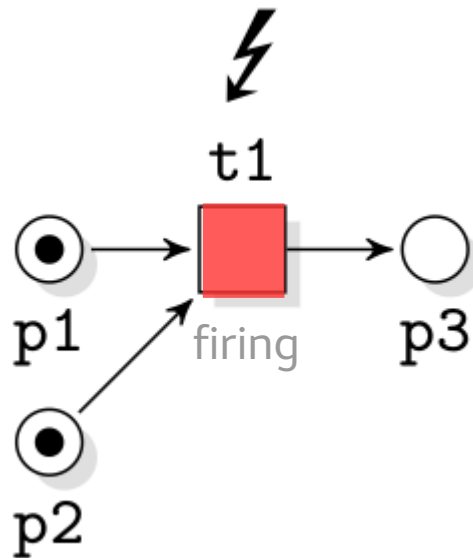
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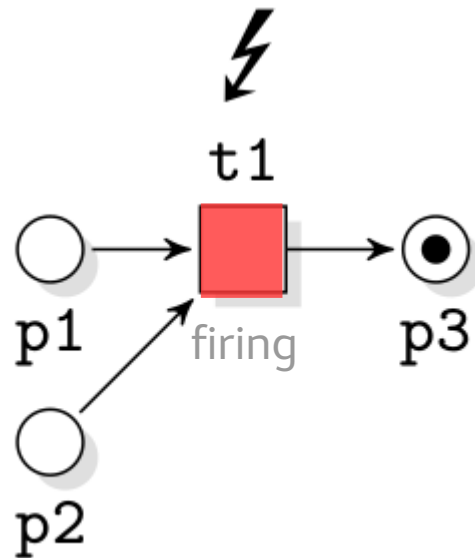
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- Execution semantics (*token game*): when the transition **fires** it will **consume** tokens from the **input** places.

# Procedural LPPN

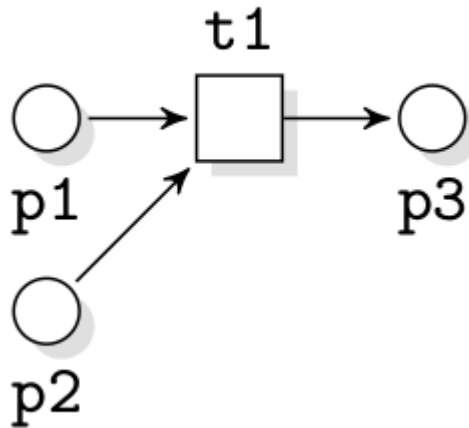
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- Execution semantics (*token game*): ...and **produce** tokens in the **output** places.

# Procedural LPPN

(same as Condition/Event PN)

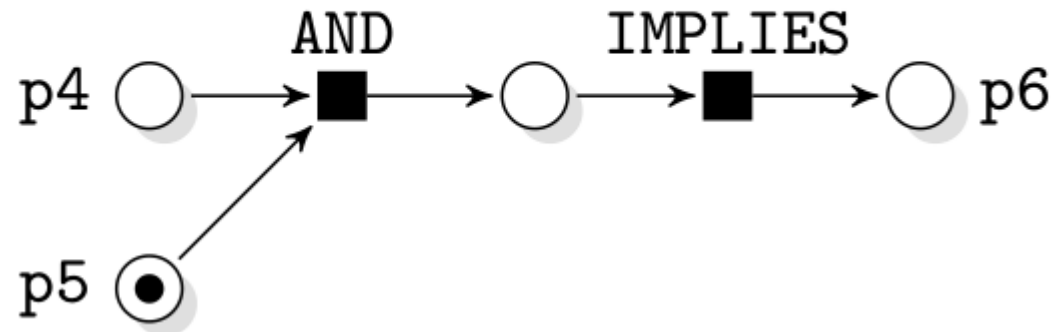


- For our purposes, this maps to a reactive rule (ECA):

$\#t1 : p1, p2 \Rightarrow -p1, -p2, +p3.$

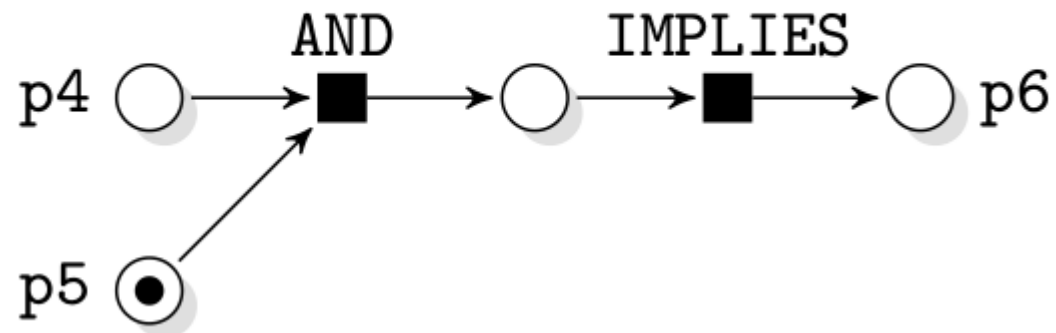


# Declarative LPPN for places



- Constructed from the ASP program:  
p6 :- p4, p5.  
p5.

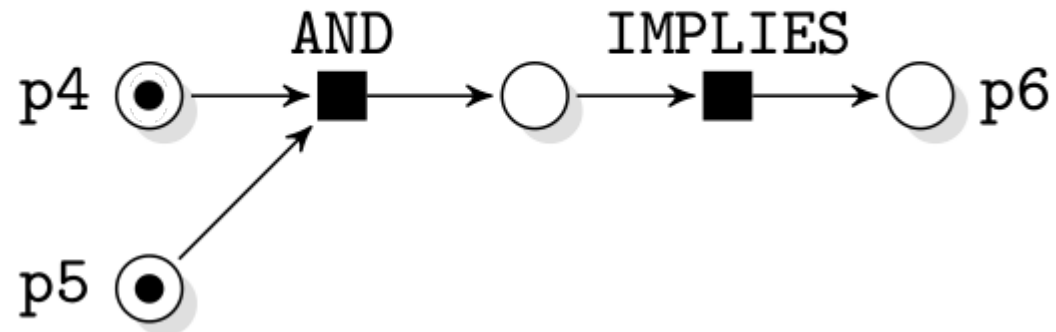
# Declarative LPPN for places



- Equivalent to  
 $p6 \text{ :- } p4, p5.$   
 $p5.$

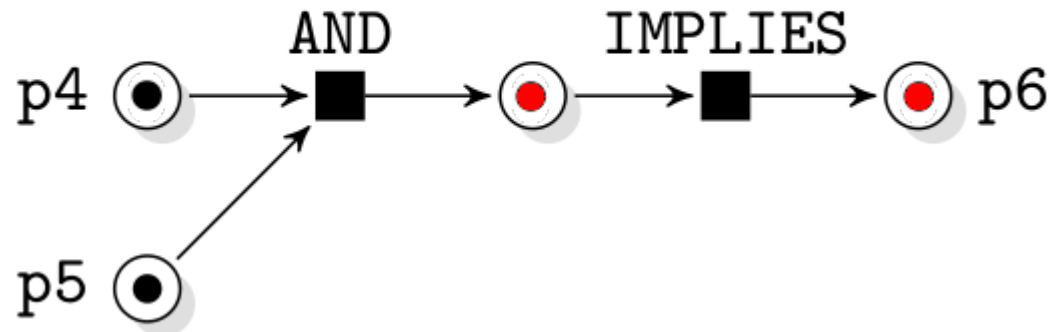
*entails*  
  
answer set  $p5.$

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# Declarative LPPN for places



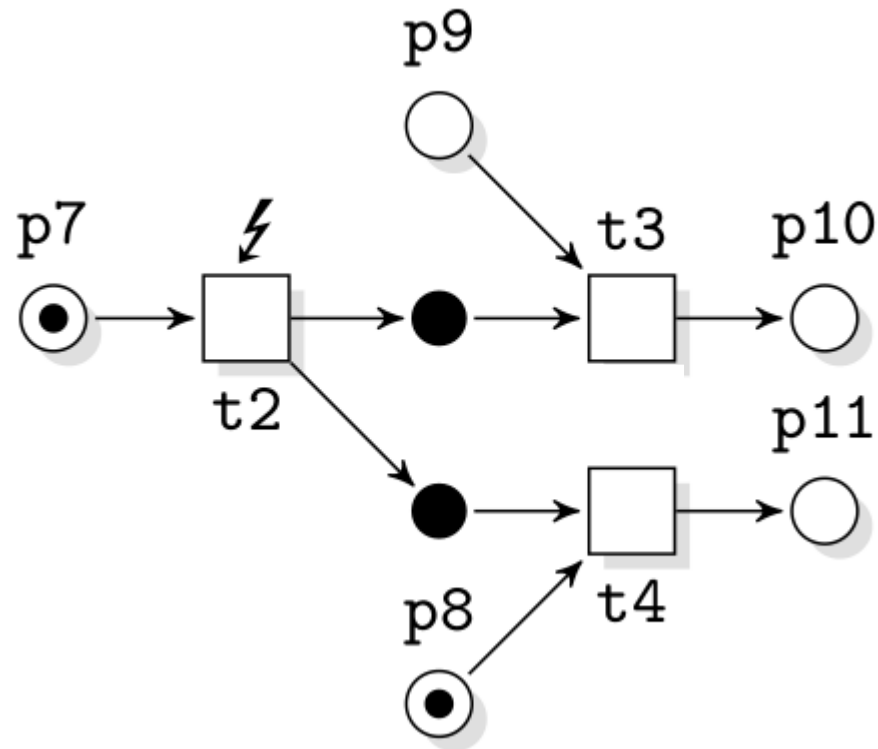
- Equivalent to  
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*entails*



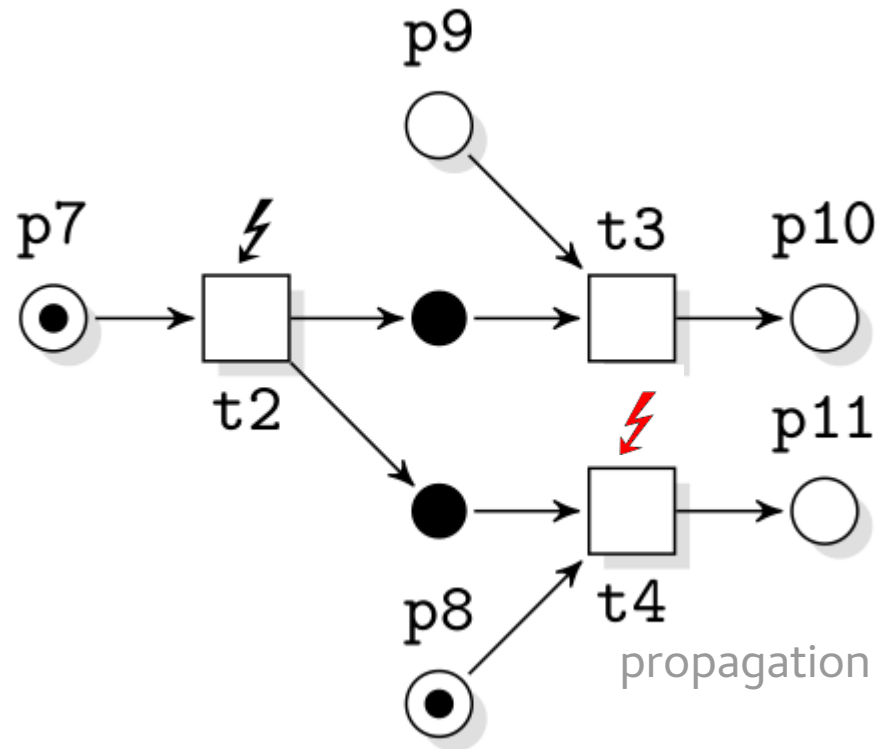
$p4. p5. p6.$

# Declarative LPPN for transitions



- Equivalent to  
 $\#t3 \text{ :- } \#t2, p9.$   
 $\#t4 \text{ :- } \#t2, p8.$   
 $\#t2. p7. p8.$

# Declarative LPPN for transitions



- Equivalent to

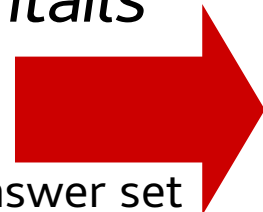
$\#t3 \text{ :- } \#t2, p9.$

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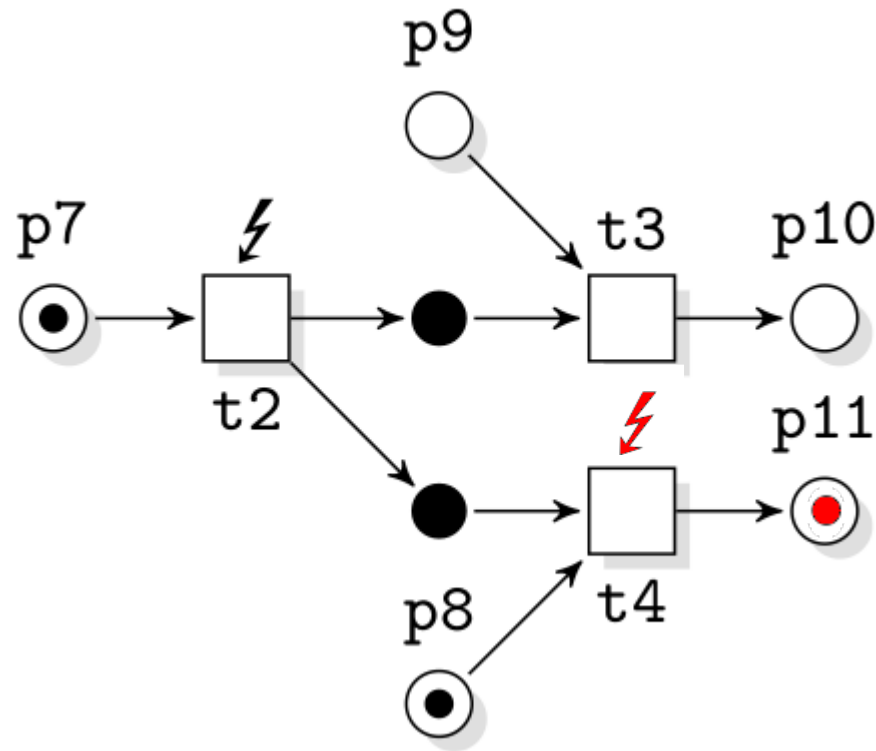
*entails*

answer set



$\#t2. p7. p8. \#t4.$

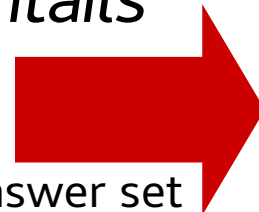
# Declarative LPPN for transitions



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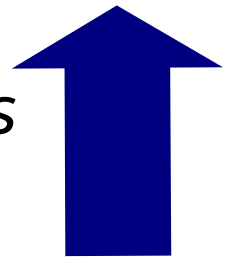
*entails*

answer set



#t2. p7. p8. #t4.

*produces*



p11.





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  - a **hybrid semantics**, consisting of 4 steps:
    1. solve logical dependencies of objects → **ASP solver**
    2. select one enabled transition to fire **direct computation**
    3. solve logical dependencies of events → **ASP solver**
    4. execute the selected firing using the Petri Net **direct computation**

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**Question: how they compare in terms of computational performance?**

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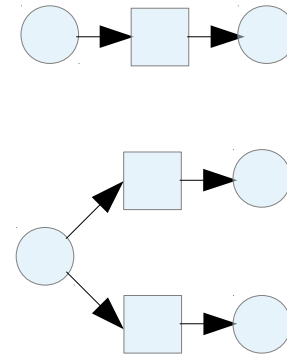
**Question: how they compare in terms of computational performance? Why they should differ?**

# Experiment

# Experiment

- We considered two basic reiterable structures at process level:

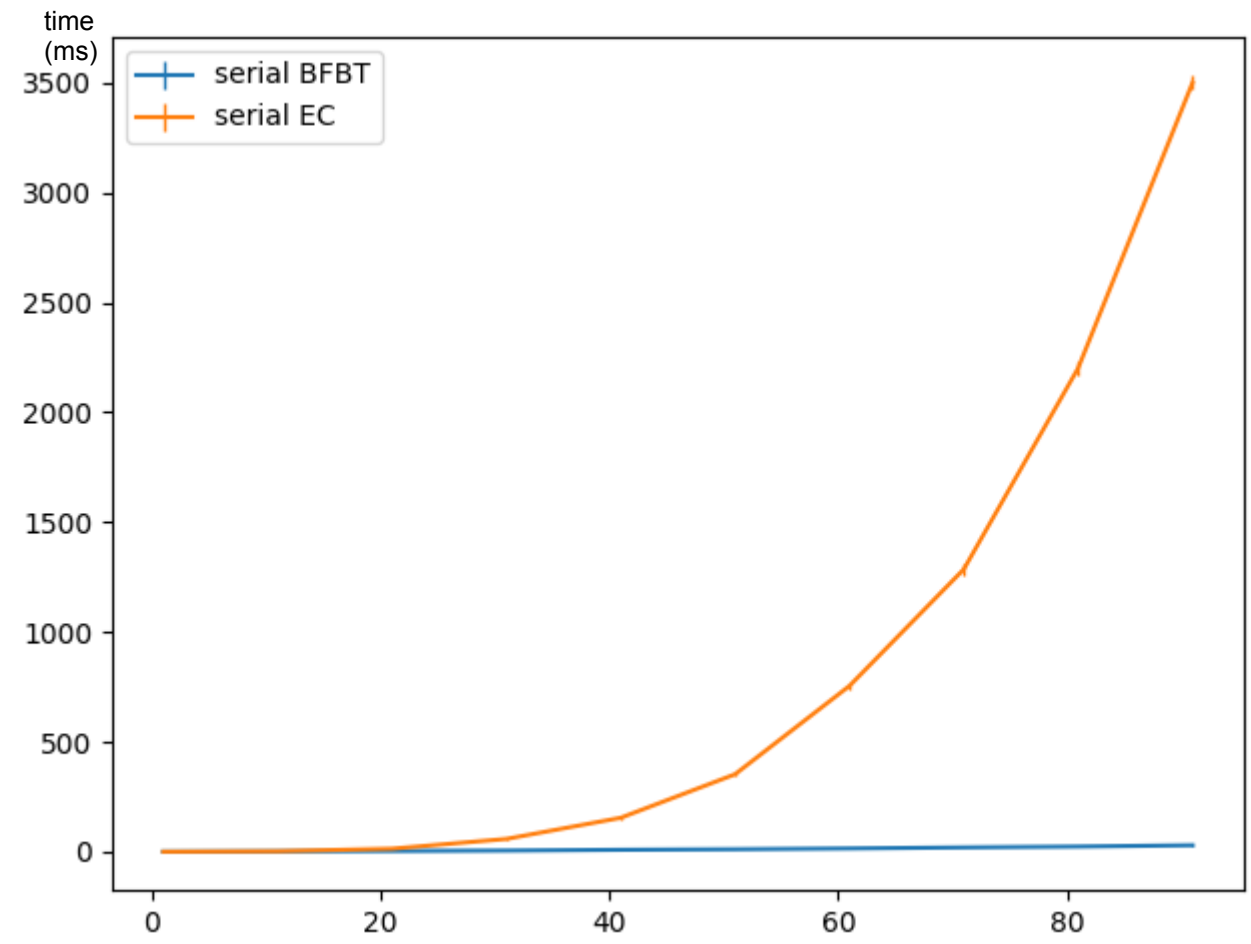
- Serial composition (deterministic)
- Forking (non-deterministic)



- We executed a benchmark on nets obtained by iterating these basic structures, with one token in the initial place
  - for N iterations = 1, 11, ..., 91 (serial)
  - for N iterations = 1, 2, ..., 10 (forking)

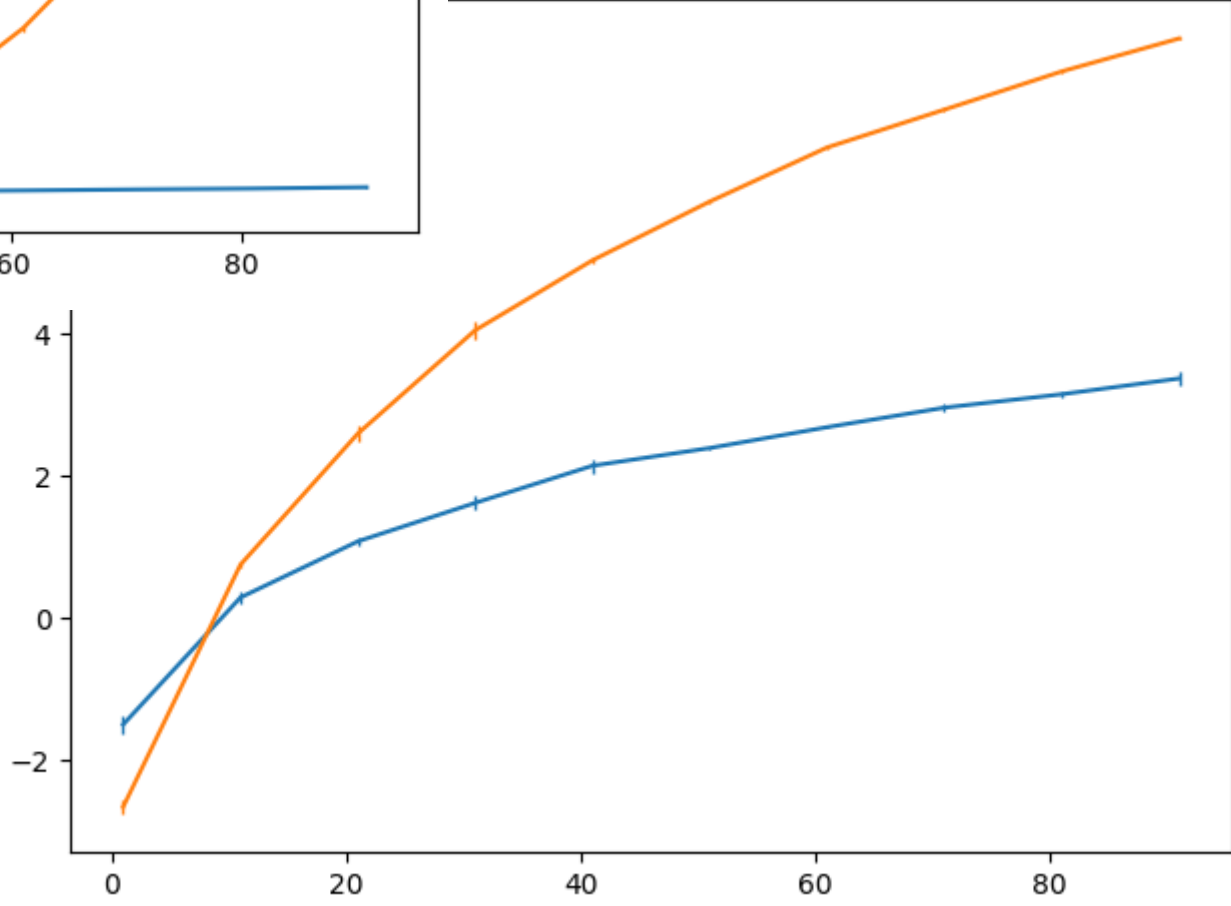
# Results

## Serial composition



Linear scale

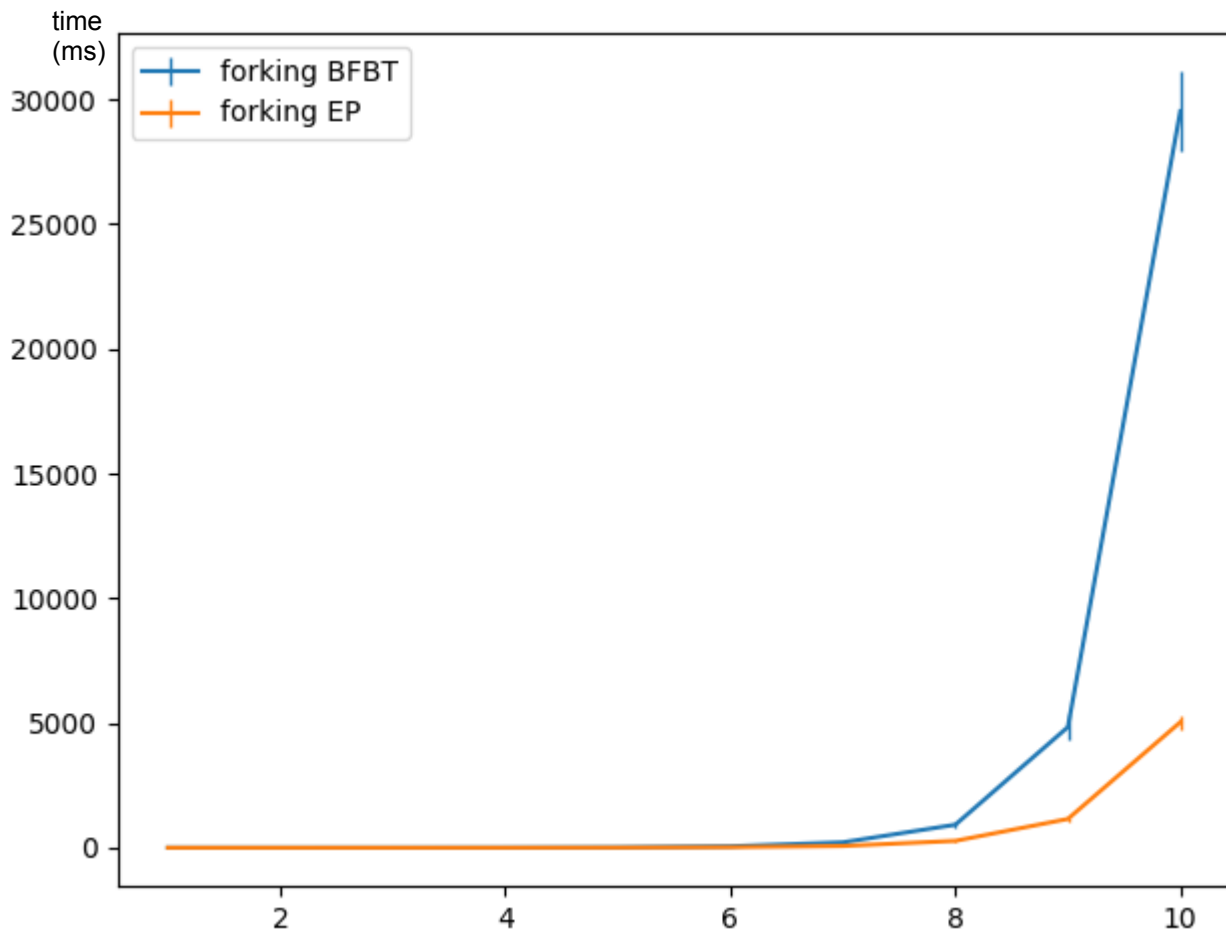
Log scale



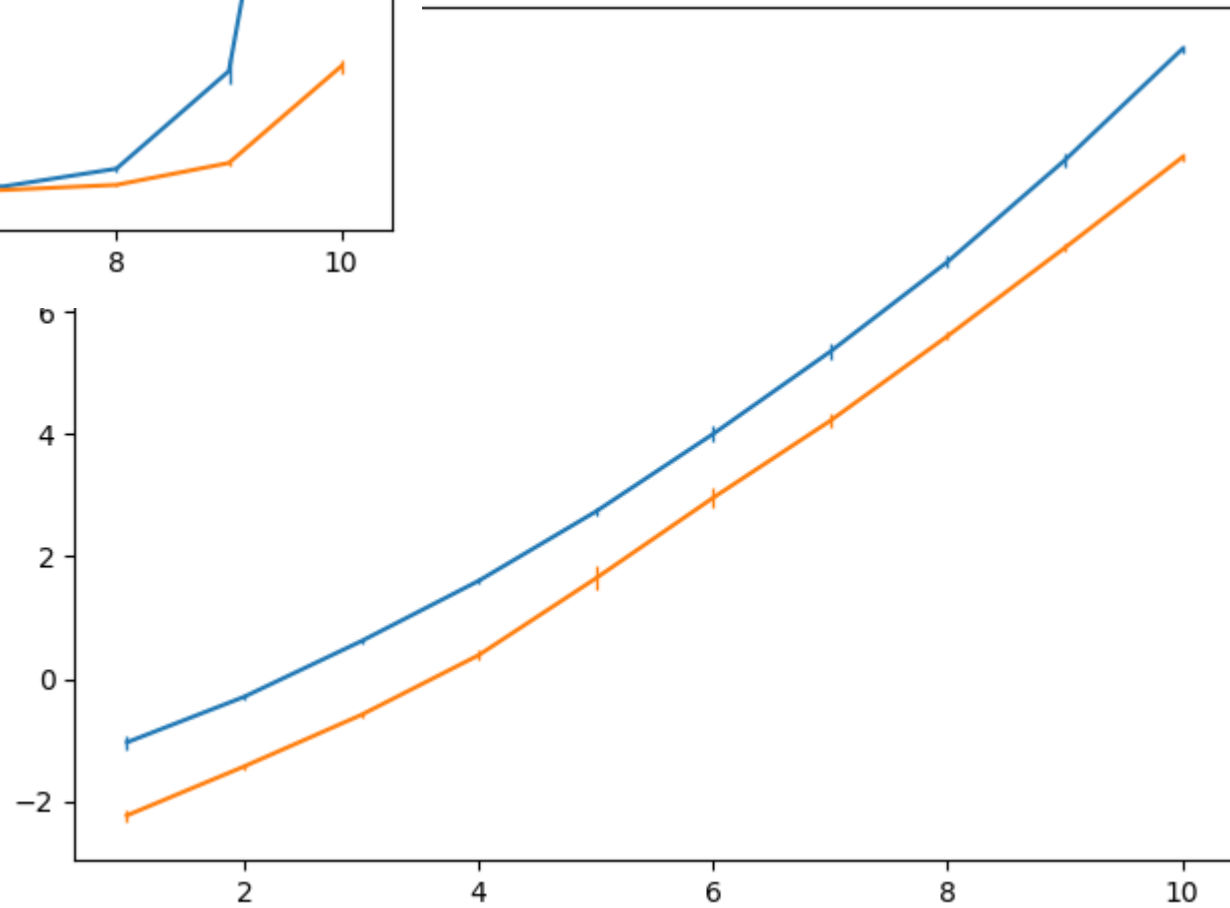


# Results

## Forking composition



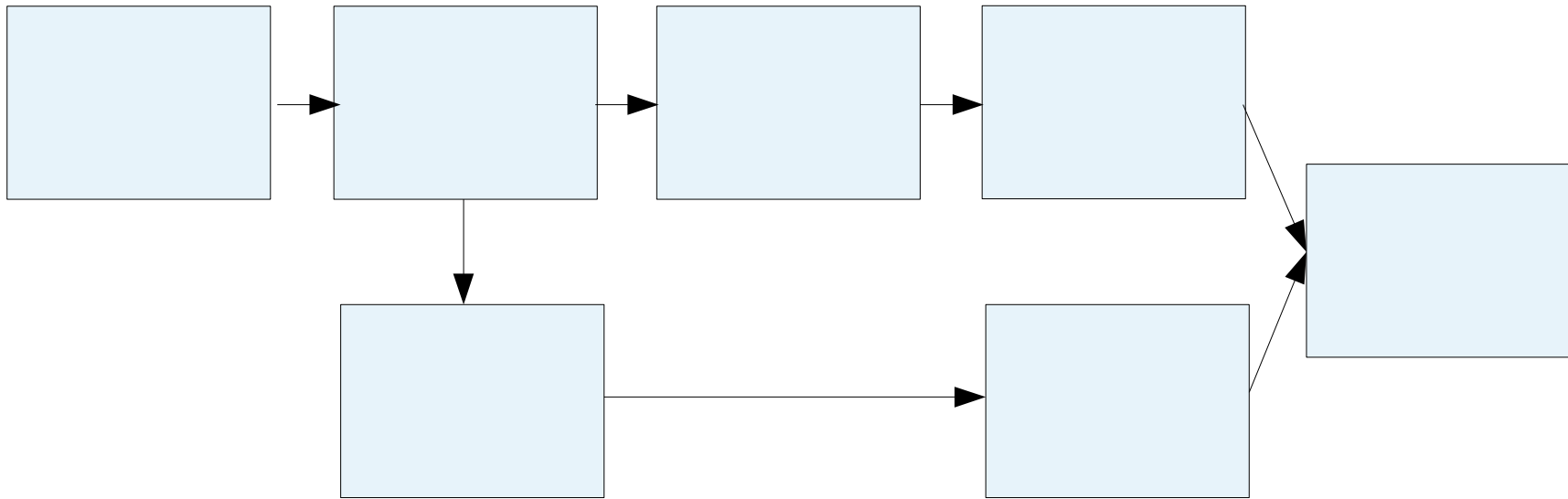
Linear scale



Log scale

Why this difference? (intuition)

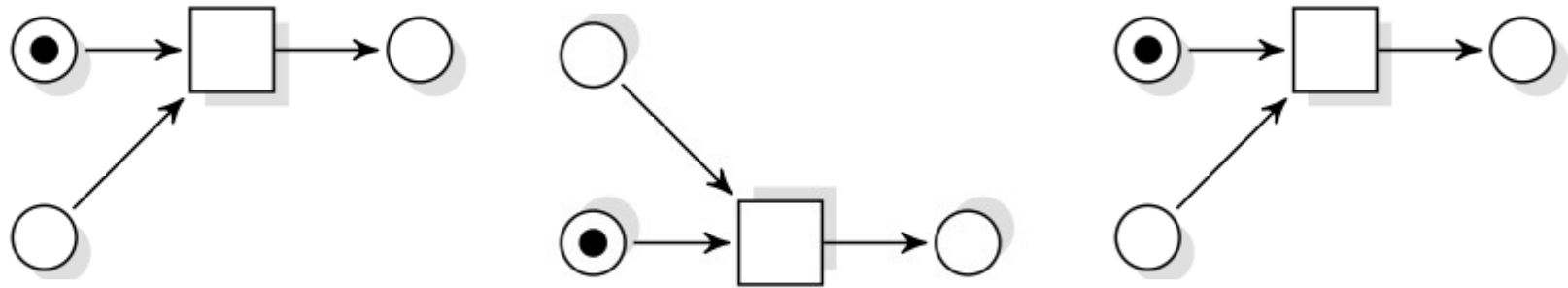
# Denotational semantics: Model execution as *search*



- Situation Calculus, Event Calculus, Fluent Calculus all rely on some form of *timestamp*.
- Causal mechanisms are mapped to logical dependences between *timestamped snapshots*

***Causation in model => Logical constraints***

# Hybrid semantics: Model execution as *execution*



- Petri nets do not require to reify the global state to perform execution.
- They are directly mappable to individual instructions in imperative programs, they utilize some (local) input to produce some (local) output.

***Causation in model => Computational causation***

# Conclusion

- The paper presents an empirical experiment with LPPNs, a *logic programming-based* extension of Petri Nets.
- LPPNs were introduced with a practical goal: a visual modelling notation, relatively simple for non-experts, handling declarative and procedural aspects of the target domain.
- Here the focus has been put on their computational properties, showing that **maintaining the two levels separated** has the potential to **bring better performances**. *The benchmark needs to be extended.*

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- *Future developments:* extension to predicate logic, optimization of execution model, “canonic” models



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